
Iterative Linear Solvers and Parallelization @ HLRS

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Iterative Linear Solvers & Parallelization @HLRS – 1st day

Content

MPI on beginners' level



[Tobias Haas and Rolf Rabenseifner]

1. MPI Overview
2. Process model and language bindings
3. Messages and point-to-point communication
4. Nonblocking communication

File: [mpi_3.1_rab.pdf](#)

Schedule

08:45 Login to ZOOM (hybrid course only)
(and establishing the break-out rooms)

09:00 Welcome

09:05 Lectures and exercises on MPI
(including some breaks)

12:30 Lunch break

13:45 Lectures and exercises on MPI
(including some breaks)

16:45 End

After the course:

S-Bahn to the city (self-paying)

City sightseeing walking tour (free)

Dinner (self-paying)

Iterative Linear Solvers & Parallelization @HLRS – 2nd day


Content

Shared memory parallelization with OpenMP [Lucienne Dettki and Rolf Rabenseifner]


Overview 

Execution model 

Worksharing directives 

Worksharing – continued (Exe 2b) 

Data environment 

Heat example (homework) 

Summary 

Pitfalls 

Q&A

Schedule

08:45 Login to ZOOM (hybrid course only)

09:00 Lectures and exercises on OpenMP
(including some breaks)

12:30 Lunch break

13:45 Lectures and exercises on OpenMP
(including some breaks)

16:45 Final end






File: [openmp-intro13.pdf](#)

Iterative Linear Solvers & Parallelization @HLRS – 3rd day

Content

Iterative Solvers for Large Linear Systems [Andreas Meister]

Files: in **Lectures_Original_Version** (with animation)
and **Lectures_Print_Version** (without animation)
and [exercises_matlab.pdf](#)

- 9:00 Introduction, Basics and Practicals (Lecture I. + Practicals)
- 10:00 Consistency and Convergence (Lecture I. continued)
- 11:00 **Break**
- 11:30 Jacobi Method (Lecture II.)
- 12:15 Practicals
- 13:00 **Lunch**
- 14:15 Gauß-Seidel Method (Lecture II. continued)
- 14:45 Practicals
- 15:15 Q+A
- 15:30 **Break**
- 15:45 **MPI:**
 - 6-(1) Collective Communication     
 - File: [mpi 3.1 rab.pdf](#)
- 16:45 **End**


Schedule

- 08:45 Login to ZOOM (hybrid course only)
- 09:00 Lectures & exercises on Iterative Solvers (including some breaks)
- 13:00 **Lunch break [30 Minutes later!]**
- 14:15 Lectures & exercises on Iterative Solvers (including some breaks)
- 15:30 **Other options on MPI**
- 16:45 **Final end**

Iterative Linear Solvers & Parallelization @HLRS – 4th day

Content

Iterative Solvers for Large Linear Systems [Andreas Meister]

- 9:00 Relaxation Schemes (Lecture II. continued)
- 10:00 Practicals
- 10:45 Break
- 11:00 Method of Steepest Descent (Lecture III.)
- 11:30 Practicals
- 12:00 Lunch
- 13:15 Method of Conjugate Gradients (Lecture III.)
- 14:15 Practicals
- 15:00 Q+A
- 15:15 Break
- 15:30 **MPI & OpenMP:**
Parallelization of Explicit and Implicit Solvers (talk) 
- File: [parallelization_rab.pdf](#)
- 16:45 End

Schedule

- 08:45 Login to ZOOM (hybrid course only)
- 09:00 Lectures & exercises on Iterative Solvers (including some breaks)
- 12:00 Lunch break [30 Minutes earlier!]
- 13:15 Lectures & exercises on Iterative Solvers (including some breaks)
- 15:30 For MPI & OpenMP: Parallelization
- 16:45 Final end

Iterative Linear Solvers & Parallelization @HLRS – 5th day

Content

Iterative Solvers for Large Linear Systems [Andreas Meister]

09:00 Introduction to Multigrid Methods (Lecture IV.)

10:00 Practicals

10:30 **Break**

10:45 GMRES and BICG (Lecture V.)

11:45 Practicals

12:15 **Lunch**

13:30 Variants of BICG (Lecture V. continued)

14:00 Practicals

14:30 Preconditioning (Lecture VI.)

15:30 Q+A

15:45 **Break**

16:00 **MPI:** 12. Derived datatypes (talk w/o practical)

(1) transfer any combination of typed data

File: [mpi 3.1 rab.pdf](#)



16:30 Q+A / **Feedback**

16:45 **End**

Schedule

08:45 Login to ZOOM (hybrid course only)

09:00 Lectures & exercises on Iterative Solvers
(including some breaks)

12:15 Lunch break [15 Minutes earlier!]

13:30 Lectures & exercises on Iterative Solvers
(including some breaks)

16:00 **Other options on MPI**

16:30 Feedback

16:45 Final end

Organizational remarks

- Laptops: do not close them (otherwise all files are lost)
- Lunch: Mensa (nearest canteen / cafeteria)
- Breaks: please do **not** take any drinks or food into the seminar room
(only empty cups are allowed for re-use in next break)
- First day: Social event
 - self paying – not included in the registration fee
 - Free tour starts immediately after the course
- Exercises



Important: To solve the exercises please **use presented slides and the provided .c/.f90 skeleton files**
(or in rare cases also the MPI standard)

but **no google search on the web** – otherwise you are too slow



– Options:

- **Work together with your neighbor**
- **Work for your own and discuss problems and compare results with your neighbor**

Please do not look at the solution before you finished this exercise,
otherwise,

90% of your learning outcome may be lost



– When finished the **basic** exercise: **advanced exercises versus coffee break**

Links

- **Course-Announcements**

- German portals:
 - www.hlrs.de/training/ (by HLRS), by [JSC](#) and [LRZ](#).
 - [Gauss Centre of Supercomputing \(GCS\) Event List](#)
 - [German HPC Calendar](#) (by [Gauss-Allianz](#) & German HPC / NHR Centers) + [long list with abstracts](#)
- European portals: [HPC in Europe](#), [CoE Training Registry](#), and [EuroCC2 training](#).

- **Self-study materials**

- <https://www.hlrs.de/training/self-study-materials/>
 - **Password-free: latest MPI slides & all exercises**
 - <https://www.hlrs.de/training/self-study-materials/MPI-course-material>
 - **With password (i.e., only for members of the HLRS email list)**
 - **MPI-Course** (2024/2023/2022) with [English](#) / [German](#) recordings (including Python)
 - **OpenMP-Course** (2023/2022) with [English](#) / [German](#) recordings

- **Standards (MPI, OpenMP)**

- www.mpi-forum.org → MPI documents (see also errata document)
- www.openmp.org → OpenMP Specifications

- **Practical (skeletons, solutions)**

- <https://fs.hlrs.de/projects/par/events/2025/ITER-HLRS/README.html>
- (https://fs.hlrs.de/projects/par/par_prog_ws/practical/README.html)

Summary — Iterative Linear Solver & Parallelization

- Iterative Linear Solver
- Parallel Programming:
 - MPI – **Distributed Memory Parallelisierung**
 - OpenMP – **Shared Memory Parallelisierung**
 - MPI-3.1/4.0 and OpenMP-4.0/4.5/5.0 advanced features
 - Parallelization
 - Slides + Practicals: <https://fs.hlrs.de/projects/par/events/2025/ITER-HLRS/README.html>
 - Further workshops and courses:
 - www.hlrs.de/training/
 - www.hlrs.de/training/self-study-materials/ (Self-Study Materials)



**Many thanks for your interest
and strong collaboration**

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